

① calculer $I = \int_{-1}^0 \frac{x+3}{x^2+4x+4} dx$ (3)

② $D = \{(x,y) \in \mathbb{R}^2, x \geq 0, y \geq 0, x+y \leq 2\}$

① tracer D

② calculer l'aire de D (en utilisant les intégrales doubles)

③ calculer $I = \iint_D (x-y)^5 dx dy$

— Bon courage —

Tel

①

$$I = \int_{-1}^0 \frac{x+3}{x^2+4x+4} dx$$

$$\frac{x+3}{x^2+4x+3} = \frac{A}{x+2} + \frac{B}{(x+2)^2}$$

$$= \frac{Ax + 2A + B}{x^2 + 4x + 3}$$

$$\begin{cases} A = 1 \\ 2A + B = 3 \end{cases} \Rightarrow \begin{cases} A = 1 \\ B = 1 \end{cases}$$

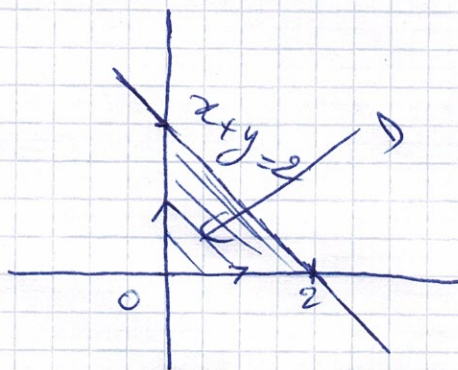
$$I = \int_{-1}^0 \left(\frac{1}{x+2} + \frac{1}{(x+2)^2} \right) dx$$

$$= \left[\ln(x+2) - \frac{1}{x+2} \right]_{-1}^0$$

$$= \frac{2 \ln(2) + 1}{2}$$

②

①



$$\begin{aligned} \textcircled{2} \text{ Area}(D) &= \iint_D dx dy \\ &= \int_0^2 \left[\int_0^{2-y} dx \right] dy \\ &= \int_0^2 (2-y) dy \end{aligned}$$

①

$$\text{Ans (1)} = \left[2y - \frac{1}{2}y^2 \right]_0^2 = 2$$

$$\begin{aligned} \textcircled{3} \quad I &= \iint_{\Delta} (x-y)^5 dx dy \\ &= \int_0^2 \left(\int_0^{2-y} (x-y)^5 dx \right) dy \\ &= \int_0^2 \left[\frac{1}{6} (x-y)^6 \right]_0^{2-y} dy \\ &= \int_0^2 \left(\frac{1}{6} (2-2y)^6 - \frac{1}{6} y^6 \right) dy \\ &= \frac{1}{6} \left[-\frac{1}{2} \times \frac{1}{7} (2-2y)^7 - \frac{1}{7} y^7 \right]_0^2 \\ &= -\frac{1}{42} \left[\frac{1}{2} (2-2y)^7 + y^7 \right]_0^2 \\ &= 0 \end{aligned}$$